

## Definable relations in Turing degree structures

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### Abstract

In this paper we investigate questions about the definability of classes of  $n$ -computably enumerable (c. e.) sets and degrees in the Ershov difference hierarchy. It is proved that the class of all c. e. sets is definable under the set inclusion  $\hat{\leq}$  in all finite levels of the difference hierarchy. It is also proved the definability of all  $m$ -c. e. degrees in each higher level of the hierarchy. Besides, for each level  $n$ ,  $n \geq 2$ , of the hierarchy a definable non-trivial subset of  $n$ -c. e. degrees is established. © 2014 Allerton Press, Inc.

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### Keywords

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